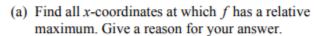
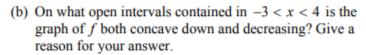
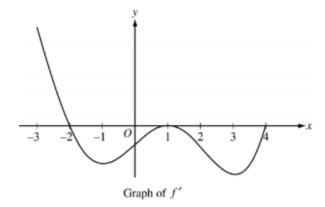
Analysis Classwork

1.

The figure above shows the graph of f', the derivative of a twice-differentiable function f, on the interval [-3, 4]. The graph of f' has horizontal tangents at x = -1, x = 1, and x = 3. The areas of the regions bounded by the x-axis and the graph of f' on the intervals [-2, 1] and [1, 4] are 9 and 12, respectively.





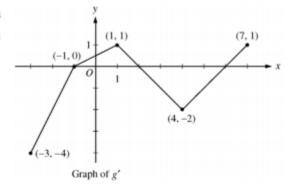


- (c) Find the x-coordinates of all points of inflection for the graph of f. Give a reason for your answer.
- (d) Given that f(1) = 3, write an expression for f(x) that involves an integral. Find f(4) and f(-2).

2.

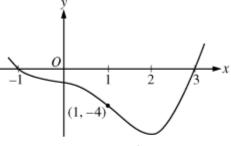
Let g be a continuous function with g(2) = 5. The graph of the piecewise-linear function g', the derivative of g, is shown above for $-3 \le x \le 7$.

- (a) Find the x-coordinate of all points of inflection of the graph of y = g(x) for −3 < x < 7. Justify your answer.
- (b) Find the absolute maximum value of g on the interval $-3 \le x \le 7$. Justify your answer.
- (c) Find the average rate of change of g(x) on the interval -3 ≤ x ≤ 7.



(d) Find the average rate of change of g'(x) on the interval $-3 \le x \le 7$. Does the Mean Value Theorem applied on the interval $-3 \le x \le 7$ guarantee a value of c, for -3 < c < 7, such that g''(c) is equal to this average rate of change? Why or why not?

Let f be a twice-differentiable function defined on the interval -1.2 < x < 3.2 with f(1) = 2. The graph of f', the derivative of f, is shown above. The graph of f' crosses the x-axis at x = -1 and x = 3 and has a horizontal tangent at x = 2. Let g be the function given by $g(x) = e^{f(x)}$.

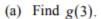


Graph of f'

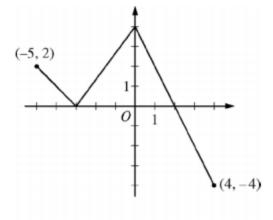
- (a) Write an equation for the line tangent to the graph of g at x = 1.
- (b) For -1.2 < x < 3.2, find all values of x at which g has a local maximum. Justify your answer.
- (c) The second derivative of g is $g''(x) = e^{f(x)} [(f'(x))^2 + f''(x)]$. Is g''(-1) positive, negative, or zero? Justify your answer.
- (d) Find the average rate of change of g', the derivative of g, over the interval [1, 3].

4.

The function f is defined on the closed interval [-5, 4]. The graph of f consists of three line segments and is shown in the figure above. Let g be the function defined by $g(x) = \int_{-3}^{x} f(t) dt$.



- (b) On what open intervals contained in −5 < x < 4 is the graph of g both increasing and concave down? Give a reason for your answer.
- (c) The function h is defined by $h(x) = \frac{g(x)}{5x}$. Find h'(3).
- (d) The function p is defined by $p(x) = f(x^2 x)$. Find the slope of the line tangent to the graph of p at the point where x = -1.



Graph of f